## Exercise 21

Use graphs to discover the asymptotes of the curve. Then prove what you have discovered.

$$
y=\frac{\cos ^{2} x}{x^{2}}
$$

## Solution

Below is a graph of the function versus $x$.


To determine the vertical asymptote(s), set what's in the denominator equal to zero and solve for $x$.

$$
\begin{aligned}
x^{2} & =0 \\
x & =0
\end{aligned}
$$

To determine the horizontal asymptote(s), find the limit of the function as $x \rightarrow \pm \infty$.

$$
\lim _{x \rightarrow \pm \infty} \frac{\cos ^{2} x}{x^{2}}=0
$$

Therefore, the horizontal asymptote is $y=0$.

